# University Of California, Berkeley Department of Mechanical Engineering

# ME 284-Nonlinear Theory of Elasticity (3 Units)

#### **Graduate Course**

#### Syllabus

### **CATALOG DESCRIPTION**

Fundamentals of the nonlinear theory of elasticity. Material symmetry. Exact solutions in elastostatics. Internal constraints. Useful strain-energy functions. Uniqueness. Compatibility conditions. Volterra dislocations. The Eshelby tensor. Small deformations superposed on finite deformations. Waves in pre-stressed solids. Stability. Bifurcations and buckling. Acceleration waves. Entropic elasticity.

#### **COURSE PREREQUISITES**

ME 185 or consent of instructor.

## **TEXTBOOK(S) AND/OR OTHER REQUIRED MATERIAL :**

None (reading assigned by instructor)

### **COURSE OBJECTIVES:**

To provide students with a working knowledge of elasticity.

### **DESIRED COURSE OUTCOMES:**

Ability to embark on modern research in the field.

### **TOPICS COVERED:**

- 1. Introduction: The nonlinear and linear field theories.
- 2. Review of relevant continuum mechanics.
- 3. Mathematical idealizations of an elastic material. Experiments, Cauchy and Green elasticity. Thermodynamical aspects.
- 4. Invariance requirements.
- 5. Material symmetry: Isotropy and anisotropy.
- 6. The initial-boundary-value problem. Some exact solutions.
- 7. Internally constrained materials: Incompressibility, inextensibility.
- 8. Useful strain-energy functions. Solutions and applications.
- 9. Universal relations of use in experimental verification. Controllable deformations. Ericksen's theorem.

10. Compatibility conditions.

11. Volterra dislocations.

- 12. The Eshelby tensor.
- 13. Small deformations superposed on large deformations. Waves in prestressed solids.
- 14. Stability criteria and their implications for constitutive equations. Material instabilities.
- 15. Bifurcations and buckling.
- 16. Acceleration waves.
- 17. Thermoelasticity. Entropic elasticity of rubber and polymers.

# **CLASS/LABORATORY SCHEDULE**

3 hours of lecture per week, 0-1 hour of discussion per week.

## ASSESSMENT OF STUDENT PROGRESS TOWARD COURSE OBJECTIVES:

40% Homework; 50% Course Project; 10% Class participation

# PERSON(S) WHO PREPARED THIS DESCRIPTION

Professor James Casey, 15 January 2016

ABBREVIATED TRANSCRIPT TITLE (19 SPACES MAXIMUM): NONLIN ELASTICITY TIE CODE: LECT GRADING: Letter and/or Pass Not Pass SEMESTER OFFERED: Fall or Spring COURSES THAT WILL RESTRICT CREDIT: None INSTRUCTORS: Staff DURATION OF COURSE: 14 weeks EST. TOTAL NUMBER OF REQUIRED HRS OF STUDENT WORK PER WEEK: 9 IS COURSE REPEATABLE FOR CREDIT? No CROSSLIST: None